



Immigration, fertility, and human capital: A model of economic decline of the West

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ABSTRACT

I show how the influences of unskilled immigration, differential fertility between immigrants and the local indigenous population, and incentives for investment in human capital combine to predict the decline of the West. In particular, indigenous low-skilled workers lose from unskilled immigration even if the indigenous low-skilled workers do not finance redistribution, do not compete with immigrants in the labor market, and do not compete with immigrants for publicly financed income transfers. For the economy at large, high-fertility unskilled immigrants and a low-fertility indigenous population result in economic decline through reduced human capital accumulation and reduced growth of per-capita output.

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1. Introduction

In European countries the total fertility rate among indigenous populations has long been far below the replacement level of 2.1 children per woman. In recent times the average total fertility rate in Europe has been 1.4 children per woman. At the same time, the reproduction rate among immigrant populations and their European-born descendants has been higher and above the replacement level. The demographic trends if continued herald the decline of the indigenous European populations to levels from which recovery is near impossible. The trends are also associated with decline in supply of high-income high-skilled labor, which forms a principal tax base for public finance. Against the background of these issues, I consider the political economy of relations between immigrants and indigenous or local population, in particular the less educated segments of local populations.

Both economic reasons and non-economic considerations such as cultural differences (for example relating to treatment of women) have also been noted as reasons for opposition to immigration. See Hillman (1994), Hillman and Weiss (1999a), Bauer et al. (2000), Hansen (2003), Dustmann and Preston (2001, 2006, 2007), Scheve and Slaughter (2001), Gang et al. (2002), O'Rourke and Sinnott (2006), Miguet (2008), among others. In this paper, I focus only on the economic aspects of immigration.

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Much immigration is illegal. I do not consider illegal immigration in this paper but focus on legal migration and the political economy of immigration policy and its long-run consequences.¹

The principal economic reason for opposition of low-skilled indigenous workers to immigration is usually portrayed as competition in the labor market that reduces the low-skilled wage. However, immigrants often do not integrate into the work force but rather remain unproductive and so do not reduce the low-skilled wage. I do not consider the reasons why parts of immigrant population remain unproductive: [Nannestad \(2009\)](#) reviews possible reasons. I show how, when immigrants do not compete in the local labor market, low-skilled workers who do not pay taxes to finance income transfers to immigrants nonetheless lose from the presence of immigrants through the relationship between fertility and human capital investment.

I link immigration-induced redistribution to reductions in fertility of the indigenous population, high fertility of the immigrants, and low attractiveness of human capital investment. With high-fertility unskilled immigrants and a low-fertility indigenous population, income transfers to immigrants raise fertility of the immigrants while decreasing fertility of the indigenous skilled population that finances the income transfers. Human capital accumulation and the growth of per-capita income decline. Immigration-induced income redistribution, although financed by taxes on the skilled workers, disadvantages the local unskilled workers through the disincentive for investment in human capital. Indigenous unskilled workers lose from the presence of immigrants, although they do not finance redistribution and do not compete with immigrants for publicly financed income transfers. Due to the differential fertility and skills, economic decline takes place among the entire population. As a consequence, without reference to the non-economic considerations, income redistribution to immigrants is the reason for opposition to immigration, especially among indigenous low-skilled workers.

To demonstrate these relationships and conclusions, I use a growth model with endogenous fertility as developed in [Dahan and Tsiddon \(1998\)](#) and [Azarnert \(2004\)](#). I describe an economy populated by two indigenous groups, one consisting of low-income unskilled workers and the other of high-income skilled workers. An unskilled minority group comprised of immigrants and their descendants is also present. The latter receive tax-financed income transfers because of insufficient own-earned income. The local unskilled workers, who earn lower wages than the skilled workers, are exempt from taxation. However, if they invest in human capital, they join the skilled and begin paying taxes. This directly reduces their potential after-tax incomes and discourages them from acquiring human capital. With children a normal good, income redistribution raises fertility of the unskilled minority beneficiaries and lowers fertility among the taxpaying local skilled population. When growth of skilled population declines, so does the total stock of human capital. Output growth declines, as does the rate of increase in the return to human capital via a human capital externality. The decline in the rate of increase of the pre-tax gross income of the skilled is a disincentive for the indigenous unskilled population to investment in human capital. The transition of the indigenous unskilled population to being skilled is thereby delayed.

2. Background empirical evidence

The model that I shall set out is based on the following empirical background evidence:

- (1) Immigrants are over-represented among welfare beneficiaries.

The evidence, from the United States, Germany, and Scandinavia, includes [Borjas \(1994a, 1999\)](#), [Borjas and Hilton \(1996\)](#), [Riphahn \(2004\)](#), [Hansen and Lofstrom \(2003, 2009\)](#), [Nannestad \(2004\)](#). For example, an immigrant family that came to Germany during ten years receives a net benefit of EUR 120,000. In the case of the U.S., a non-white immigrant aged between 20–30 years on arrival with less than high school education typically imposes a net fiscal burden of approximately US\$ 100,000 in present value terms ([Razin and Sadka, 2004](#)). In Germany and Sweden, the proportion of immigrants among income support recipients has exceeded their share in the total population since at least 1980.² In Denmark, during the 1990s, an increase in non-Western immigration was associated with a sharp increase in the amount of net transfers from indigenous Danes to the public sector.³ In his survey of the literature on immigration and welfare state, [Nannestad \(2007\)](#) summarizes the evidence as concluding that immigration was disadvantageous for the indigenous population and beneficial for immigrants. The evidence indicates that European-born descendants of non-white immigrants in general do not assimilate into local labor markets and exhibit very high welfare dependency ([Nannestad, 2004](#) and references therein).⁴ In Europe, a considerable part of immigrant minorities do not

¹ [Hillman and Weiss \(1999b\)](#) describe illegal immigration that is permitted as long as an immigrant remains employed in a particular sector. I also do not consider such permissible illegal immigration. Immigrants in these cases are productive and do not receive income transfers from the state. In [Azarnert \(2010b\)](#) I consider the relationship between fertility in the host economy and the intensity of the struggle against immigration.

² For example, in 1996, the share of minority immigrants among income support recipients in Germany was 25.8%, while their share in the total population was less than 10%. In Western Germany, between 1991 and 1996 an increase in the number of minority immigrants was associated with an increase in real expenditures on income support by 141% ([Riphahn, 2004](#)). It is also noteworthy that since 1994 these statistics exclude expenditures on asylum seekers. Ethnic German immigrants from Eastern Europe are considered in these statistics as German nationals. Similarly, in Sweden, an increase in the share of immigrants in the population from 7.6% to 10.8% between 1983 and 1996 was associated with an increase in real expenditure on social assistance by 170%, while by the mid-1990s immigrants accounted to nearly half of the country's expenditure on social assistance, up from less than one quarter of total expenditures in the early 1980s ([Hansen and Lofstrom, 2009](#)).

³ Net transfers from indigenous Danes to the public sector in Danish kroner (1997 prices) per person increased from 14,900 in 1991 to 24,500 in 1998 ([Nannestad, 2004, table 2](#)). The first estimate of the fiscal impact of immigration in Denmark published in December 1997 shows that the net cost of non-Western immigrants amounted to 11.3 billion Danish kroner in 1995 ([Nannestad, 2007, note 27](#)).

⁴ [Borjas and Hilton \(1996\)](#) report that in the U.S. in the early 1990s, as compared to American Whites, Hispanics and blacks were more likely to participate in some welfare program by factors of 3 and 4 respectively.

participate in the labor market and among those who are formally in the labor force, unemployment is much higher than that among the indigenous population.⁵ Use of public employment for the purpose of disguised income redistribution toward disadvantaged minorities has also been noted (Alesina et al., 2000).

The second empirical proposition is that:

- (2) Skills and economic outcomes differ among ethnic groups.

The existence of large wage differentials between different ethnic groups after standardizing for observed skills has been well documented (Borjas, 1994a,b, 1999, among others).⁶ Within this context, Borjas (1994a, p. 1714) concludes that “current immigration in the US and in many other countries is setting the stage for ethnic differences in economic outcomes that are likely to be a dominant feature of labor market in these countries throughout the next century”. The importance of ethnicity in the process of human capital accumulation has also been well established (e.g., Borjas, 1992). More specifically, lower educational success of minorities has been broadly documented as well: for example, Light and Strayer (2006) report that US minorities, although more likely than observably equivalent Whites to attend colleges, are less likely than their White counterparts to complete college. Riphahn (2003) finds that in Germany the schooling successes of second-generation, German-born Turkish immigrants lag behind those of the indigenous population. Immigrants fail to attain educational standards of the indigenous population and increasingly fall behind. Large gaps in educational achievements between natives and second-generation nonwestern immigrants have been reported in Denmark (Nannestad, 2004 and references therein).

The third empirical proposition, to which I have referred, is that:

- (3) The less educated immigrants have higher fertility levels than the indigenous population.

3. Related literature on fertility and income redistribution

My model will combine endogenous fertility and growth with effects of redistribution on growth.⁷ According to a neoclassical economic theory of fertility, the decision to have children is a function of individuals' preferences with regard to children, subject to the costs of children and an income constraint. According to this theory, any increase in income as a result of receiving income transfers is expected to increase the demand for children, while any decrease in income as a result of paying taxes is expected to reduce the demand for children (Becker, 1981; Cigno, 1991). Recent models with endogenous fertility and the explicit quantity–quality tradeoff assume that children are a normal good for everyone, but the price of child quantity relative to that of child quality increases with labor income, giving the poor (uneducated) a comparative advantage in child quantity and the rich (educated) a comparative advantage in the child quality. These models also imply that non-labor income transfers are expected to increase fertility of the recipients, while, in contrast, taxation of labor income is expected to reduce fertility of taxpayers (Cigno, 1986; Morand, 1999; Moav, 2005; Azarnert, 2008). The impact of tax-benefit system on fertility has also been well documented empirically. See, for example, Whittington et al. (1990), Hyatt and Milne (1991), Whittington (1992), Zhang et al. (1994), Gauthier and Hatzius (1997), Milligan (2005), among others.

4. The structure of the economy

With the above empirical and theoretical background, I turn now to the model of this paper. I consider an overlapping-generation economy in which agents live for two periods and capital flows freely among countries at a fixed world interest rate r . In the first period of life, agents are children: each consumes a fixed quantity of his parents' time. Children can either perform simple tasks (unskilled work) or invest in human capital. In the second period of life, they either benefit from higher income if they invest in human capital or work as unskilled workers for lower pay. In either case, they decide on their own consumption and the number of their offspring. As parents, they bring up their children spending a fixed fraction of their net labor income per child.

The economy is populated by two groups of people: an indigenous majority group and a minority group, which comprises immigrants and their descendants who are easily distinguishable from the indigenous population. Suppose that the group of immigrants grows only through their natural reproduction and that further immigration is not allowed. Initially all minority individuals are unskilled and earn less than the local unskilled. Because of insufficient own-earned income, the minority unskilled receive financial support financed by taxes levied on the local skilled workers. The local unskilled, who earn lower wages than the skilled, are exempt from taxation, but, if they invest in human capital, they join the skilled and start paying taxes. The offspring of

⁵ Nannestad (2004) reports that in Denmark more than 50% of nonwestern immigrants and their descendants were outside the labor force in 2001. For two immigrant groups, labor-market participation rates were but 14 and 26 percent respectively. During 1985–2001, among immigrants and their Danish-born descendants, unemployment was some 3 times or more greater than that among indigenous Danes. Similarly, Algan et al. (2010) report that in France, Germany and the UK employment rates of second-generation, European-born immigrants of non-European ancestry are significantly lower than the employment rates of the indigenous populations in these countries. Moreover, for most groups of non-European immigrants, the employment rates of the second-generation male immigrants are lower than the employment rates of the first-generation male immigrants. Preferences for consumption and leisure can be a consideration. On leisure and redistribution, see Holdler (2008).

⁶ Borjas (1994b) who analyzes the convergence of ethnic skill differentials among the offspring of immigrants who arrived to the US from different European countries during the Great Migration of 1881–1910 demonstrates that after 3 generations in the US their ethnic differences narrowed, but did not disappear.

⁷ There has been much literature on growth with endogenous fertility. See Galor (2005) for a survey and Azarnert (2006, 2008, 2010b).

the minority unskilled who choose to invest in human capital join the skilled and give up the subsidy. When the offspring of the minority unskilled become skilled, the redistribution ends.⁸

4.1. Production

In period $t + 1$ production of the same aggregate output is performed in two sectors.

Production in the unskilled sector uses capital and labor with a fixed level of technology:

$$Y_{t+1}^u = A^u K_{t+1}^\alpha (L_{t+1})^{1-\alpha}, \quad (1)$$

where L_{t+1} is the number of the unskilled workers in period $t + 1$ and A^u is the fixed level of technology in this sector.

In a world where capital is free to flow at the rate of interest r , the wage of a local unskilled worker is thus fixed at:

$$w^u = A^u (1-\alpha) \left(\frac{\alpha A^u}{r} \right)^{\frac{\alpha}{1-\alpha}}. \quad (2)$$

Suppose that the unassimilated minority workers are less productive than the indigenous unskilled workers. To capture their lower productivity, suppose that they cannot exploit the whole technology available in the host economy, but only a lower technology A^m ; $A^m < A^u$.

The wage of an unassimilated minority worker is therefore fixed at:

$$w^m = A^m (1-\alpha) \left(\frac{\alpha A^m}{r} \right)^{\frac{\alpha}{1-\alpha}}, \quad (3)$$

which is lower than the wage of an indigenous local worker: $w^m < w^u$.

In general, the lower wages of the minority unskilled may result either from their lower productivity relative to the local unskilled, as here, or from a discrimination against them in the labor market. For any reason, if they receive a tax-financed income support to compensate for lower incomes, the effect is the same, and this paper is about the effect, not about reasons.

Production in the skilled sector uses capital and efficiency units of labor. The total number of efficiency units E in this sector is a weighted average of E^s , E^{us} and E^{ms} , where the weights are the numbers of s -individuals (skilled children of local skilled parents), us -individuals (skilled children of local unskilled parents), and ms -individuals (skilled children of the minority unskilled parents). I also assume that the skill premium for a child of an indigenous skilled parent is higher than that for a child of an indigenous unskilled parent, and that the skill premium for a child of an indigenous unskilled parent is higher than the skill premium for a child of a minority unskilled parent. More specifically, when investing in human capital, the child of a skilled parent obtains E^s efficiency units, while the skilled child of an indigenous unskilled parent obtains E^{us} units of efficiency, and the skilled child of an unskilled minority parent obtains only E^{ms} units of efficiency ($E^s > E^{us} > E^{ms}$).⁹ Once an individual of an unskilled ancestry of either type acquires human capital, the dynasty becomes skilled and, from the next period on, all children within this dynasty obtain E^s units of efficiency. Suppose also that the level of technology in the advanced skilled sector is higher than that in the unskilled sector and it also can increase with time.

The production function in the skilled sector is thus

$$Y_{t+1}^s = A_{t+1} K_{t+1}^\alpha E_{t+1}^{1-\alpha}, \quad (4)$$

where $E_{t+1} = L_{t+1}^s E^s + L_{t+1}^{us} E^{us} + L_{t+1}^{ms} E^{ms}$, A_{t+1} is the level of technology in the skilled sector at time $t + 1$ ($\forall t + 1, A_{t+1} > A^u$), and L_{t+1}^j is the total number of j -type adult individuals in the economy in period $t + 1$.

In a world where capital is free to flow at the rate of interest r , the return to one unit of efficiency in the skilled sector equals:

$$w_{t+1}^s = A_{t+1} (1-\alpha) \left(\frac{\alpha A_{t+1}}{r} \right)^{\frac{\alpha}{1-\alpha}}. \quad (5)$$

Suppose technological progress is a function of a past society-wide stock of human capital. To capture this effect, assume A_{t+1} is a function of the aggregate level of human capital in the economy in the previous period, $A_{t+1} = A(E_t)$. Since human capital per educated person is fixed by construction of this model, an aggregate change comes out of an increase in the population of educated persons only, which is a Kremer-type assumption; $A(\cdot) > 0, A'(\cdot) > 0, A''(\cdot) < 0$.

⁸ Imposing some moderate heterogeneity in the m -group in the sense that some small fraction of immigrants acquires education earlier than the majority of immigrants, does not alter this paper's results as long as this fraction is not too large.

⁹ There are many explanations for the parental lead in education: informal education, cultural aspect, the time spent searching for a job or quality of the match. Whatever the reasons, the empirical significance of the parental effect has been widely documented (see Rubinstein and Tsiddon, 2004 for references). Lower educational success of minorities (Riphahn, 2003; Nannestad, 2004; Light and Strayer, 2006), as well as the existence of large intergenerationally transmitted (Borjas, 1992) wage differentials between different ethnic groups (Borjas, 1994a,b, 1999) has also been well documented.

4.2. Redistribution

The minority unskilled earn less than the local unskilled. Because of insufficient own-earned income, the minority unskilled receive an income support financed by taxes levied on the wealthy local skilled. To specify the tax-transfer scheme, the following is assumed:

A1. In period $t + 1$, there is one common tax rate τ levied on the skilled.

A2. The proceeds are distributed proportionally to the number of the unskilled minority recipients.

The scheme specified above yields that the sum of transfer an adult unskilled individual receives in period $t + 1$ is

$$\varphi_{t+1} = \frac{\tau W_{t+1}^s (E^s L_{t+1}^s + E^{us} L_{t+1}^{us})}{L_{t+1}^m}, \tag{6}$$

where L_{t+1}^s is the number of skilled taxpayers (L^{us} is positive at the date when the offspring of the local unskilled switch to the skilled status and is meaningless otherwise), L_{t+1}^m is the number of unskilled minority recipients, and τ is the rate of tax.¹⁰

Given the assumption that all individuals in the minority group are alike, the redistribution will be abolished at a moment when children of the minority unskilled will find it profitable to invest in human capital and switch to skilled status.

4.3. Utility maximization

Every agent derives utility from consumption in the second period of life and from the number of his living children. There is no uncertainty. The utility function of an individual born at time t is

$$U_t = (1-\beta)\ln(C_{t+1}) + \beta\ln(N_{t+1}), \tag{7}$$

where C_{t+1} is second-period consumption and N_{t+1} is the number of living children.¹¹

Individuals in this economy are classified as: (1) s , the skilled offspring of the indigenous skilled parents, (2) u , the indigenous unskilled, (3) us , the skilled offspring of the indigenous unskilled parents, (4) m , the minority unskilled, and (5) ms , the skilled offspring of the minority unskilled.

An individual's lifetime income is allocated between consumption and childrearing. The cost of rearing children represents a fixed fraction δ of parental net labor income per each child. Given the tax-transfer scheme, as specified in Section 4.2, with the lifetime income (I_{t+1}^j) as given in Eq. (11), the budget constraint for each type of individuals is respectively:

$$\begin{aligned} C_{t+1}^s + \delta N_{t+1}^s E^s W_{t+1}^s (1-\tau) &= I_{t+1}^s, & C_{t+1}^{us} + \delta N_{t+1}^{us} E^{us} W_{t+1}^s (1-\tau) &= I_{t+1}^{us}, \\ C_{t+1}^u + \delta N_{t+1}^u W^u &= I_{t+1}^u, & C_{t+1}^{ms} + \delta N_{t+1}^{ms} E^{ms} W_{t+1}^s &= I_{t+1}^{ms}. \end{aligned} \tag{8}$$

Each individual maximizes his utility subject to his budget constraint. He has two decision variables: consumption and the number of children. For each generation t , the optimal level of each choice variable is

$$\begin{aligned} C_{t+1}^j &= (1-\beta)I_{t+1}^j, \quad j = s, u, m, us, ms, \\ N_{t+1}^s &= \frac{\beta}{\delta E^s W_{t+1}^s (1-\tau)} I_{t+1}^s, & N_{t+1}^{us} &= \frac{\beta}{\delta E^{us} W_{t+1}^s (1-\tau)} I_{t+1}^{us}, \\ N_{t+1}^u &= \frac{\beta}{\delta W^u} I_{t+1}^u, & N_{t+1}^{ms} &= \frac{\beta}{\delta E^{ms} W_{t+1}^s} I_{t+1}^{ms}, \\ N_{t+1}^m &= \frac{\beta}{\delta W^m} I_{t+1}^m, \end{aligned} \tag{9}$$

¹⁰ In this model the rate of tax is exogenous, but it can be easily endogenized as, for instance, in Azarnert (2004) where the tax is determined by the opportunities for the skilled taxpayers abroad. It can be also assumed that in the starting period the rate of tax is set in such a manner, so as to ensure that the total income of the minority unskilled, including the sum of transfer (φ_{t+1}), does not exceed the labor income of the local unskilled.

¹¹ Since the parental effect exists in human capital, a parental care for the well being of their offspring is not necessary in this context.

Using Eq. (9), the (indirect) utility function at the optimum is

$$\begin{aligned} U_t^s &= \ln(I_t^s) - \beta \ln(\delta E^s w_{t+1}^s (1-\tau)) + \varepsilon, & U_t^{us} &= \ln(I_t^{us}) - \beta \ln(\delta E^{us} w_{t+1}^s (1-\tau)) + \varepsilon, \\ U_t^u &= \ln(I_t^u) - \beta \ln(\delta w^u) + \varepsilon, & U_t^{ms} &= \ln(I_t^{ms}) - \beta \ln(\delta E^{ms} w_{t+1}^s) + \varepsilon, \\ U_t^m &= \ln(I_t^m) - \beta \ln(\delta w^m) + \varepsilon, \\ \text{where } \varepsilon &\equiv \beta \ln(\beta) + (1-\beta) \ln(1-\beta). \end{aligned} \quad (10)$$

4.4. Investment in human capital

Each individual has one unit of time in each period of life. It can be used either for education or work. As specified in Section 4.1, there exists the parental effect in human capital modeled as a wedge in the return to investment in human capital ($E^s > E^{us} > E^{ms}$). Since the parental effect in human capital is assumed to be strong enough and the rate of tax is assumed to be not too high, the offspring of skilled parents always invest in education. The offspring of unskilled parents decide in the first period whether or not to invest in human capital. An individual who chooses to invest in education spends all his working time in the first period of life at school and pays for that education a constant fraction of the gross skilled wage $h = \theta w^s$. There are no restrictions on borrowing at a fixed interest rate r . In the second period an adult individual works as a skilled worker, earning w^s per one unit of efficiency he obtained. As long as the redistribution exists, a local skilled individual pays a fraction τ of his labor income in taxes. A local individual who does not invest in human capital engages in unskilled labor in both periods of his life and earns w^u each period. A minority individual who does not invest in human capital engages in unskilled labor each period, earns each period w^m and receives income support (φ) in the second period. A minority agent who invests in education spends all his time at school in the first period, pays θw^s for that education, earns w^s per each unit of efficiency in the second period and gives up the subsidy.

Given the tax-transfer scheme, as specified in Section 4.2, for individual born at period t , the whole lifetime income in terms of second period is one of the following forms:

$$\begin{aligned} I_{t+1}^s &= E^s w_{t+1}^s (1-\tau) - \theta w_t^s (1+r), & I_{t+1}^{us} &= E^{us} w_{t+1}^s (1-\tau) - \theta w_t^s (1+r), \\ I_{t+1}^u &= w^u (2+r), & I_{t+1}^{ms} &= E^{ms} w_{t+1}^s - \theta w_t^s (1+r). \\ I_{t+1}^m &= w^m (2+r) + \varphi_{t+1}, \end{aligned} \quad (11)$$

According to Eq. (10), for each generation t , the utility is, correspondingly:

$$\begin{aligned} U_t^s &= \ln\{E^s w_{t+1}^s (1-\tau) - \theta w_t^s (1+r)\} - \beta \ln\{\delta E^s w_{t+1}^s (1-\tau)\} + \varepsilon, \\ U_t^u &= \ln\{w^u (2+r)\} - \beta \ln\{\delta w^u\} + \varepsilon, \\ U_t^m &= \ln\{w^m (2+r) + \varphi_{t+1}\} - \beta \ln\{\delta w^m\} + \varepsilon, \\ U_t^{us} &= \ln\{E^{us} w_{t+1}^s (1-\tau) - \theta w_t^s (1+r)\} - \beta \ln\{\delta E^{us} w_{t+1}^s (1-\tau)\} + \varepsilon, \\ U_t^{ms} &= \ln\{E^{ms} w_{t+1}^s - \theta w_t^s (1+r)\} - \beta \ln\{\delta E^{ms} w_{t+1}^s\} + \varepsilon. \end{aligned} \quad (12)$$

As long as $U_{t+1}^u > U_{t+1}^{us}$, children of local unskilled parents decide to remain unskilled. Once this inequality is reversed (or turned into equality), children of local unskilled parents choose to become skilled. Correspondingly, as long as $U_{t+1}^m > U_{t+1}^{ms}$, the offspring of the minority unskilled choose to remain unskilled.

4.5. Fertility choice

From Eq. (9), for a given tax rate τ , one can calculate the number of children per parent. Denoting by N_{t+1}^j the number of offspring of a parent born in period t , where $j = s, u, m, us, ms$, these numbers are

$$N_{t+1}^s = \frac{\beta}{\delta} \left[1 - \frac{\theta w_t^s (1+r)}{E^s w_{t+1}^s (1-\tau)} \right], \quad (13)$$

$$N_{t+1}^{us} = \frac{\beta}{\delta} \left[1 - \frac{\theta w_t^s (1+r)}{E^{us} w_{t+1}^s (1-\tau)} \right], \quad (14)$$

$$N_{t+1}^u = \frac{\beta}{\delta} (2+r). \quad (15)$$

Fertility choice of unskilled minority individuals depends on the transfer payments they receive. Given Eq. (6), it is

$$N_{t+1}^m = \frac{\beta}{\delta} \left((2+r) + \frac{\tau w_{t+1}^s (E^s L_{t+1}^s + E^{us} L_{t+1}^{us})}{w^m L_{t+1}^m} \right). \quad (16)$$

As I show below in Section 4.6, at some point it becomes lucrative for the offspring of the minority unskilled to give up their subsidy and switch to skilled status. Given the tax-transfer scheme, as specified in Section 4.2, at this moment taxation is abandoned. Hence, fertility for *ms*-individuals is

$$N_{t+1}^{ms} = \frac{\beta}{\delta} \left[1 - \frac{\theta w_t^s (1+r)}{E^{ms} w_{t+1}^s} \right]. \quad (17)$$

Accordingly, the reproduction rate of the local skilled parents comes back to its natural level:

$$N_{t+1}^s = \frac{\beta}{\delta} \left[1 - \frac{\theta w_t^s (1+r)}{E^s w_{t+1}^s} \right]. \quad (18)$$

Comparing the number of offspring for all of the groups in the case without redistribution and the corresponding numbers of offspring in the case under discussion, one can compute fertility gaps that appear due to redistribution.¹²

Whereas the ‘under-fertility’ among the local skilled of the skilled or unskilled ancestry is

$$\Delta N_{t+1}^j = \frac{\beta}{\delta} \left[\frac{\tau \theta w_t^s (1+r)}{E^j w_{t+1}^s (1-\tau)} \right], \text{ where } j = s, ms, \quad (19)$$

the ‘over-fertility’ among the minority unskilled is

$$\Delta N_{t+1}^m = \frac{\beta}{\delta} \left(\frac{\tau w_{t+1}^s (E^s L_{t+1}^s + E^{us} L_{t+1}^{us})}{w^m L_{t+1}^m} \right). \quad (20)$$

The main result of this section is thus immediately clear. Redistribution to the minority unskilled, financed by taxes levied on the local skilled, raises fertility among the minority beneficiaries and lowers fertility among the taxpaying local skilled population. Moreover, as shown in Eq. (19), since $E^s > E^{us}$, the under-fertility among local skilled individuals whose parents were unskilled is higher than the under-fertility among local skilled individuals whose parents were skilled.

4.6. The dynamic path

In order to examine the dynamic behavior of the economy, I first characterize the process of human capital accumulation. Next, since $E^{us} > E^{ms}$, I analyze the behavior of the corresponding groups consecutively.

4.6.1. Step 1: Human capital accumulation dynamics

Consider first the dynamics of human capital accumulation. Provided that children are viewed as a normal good, once the redistribution starts, taxation lowers fertility among the taxpaying skilled. When the number of skilled people grows slower, so does the total stock of human capital. Given the structure of the skilled sector (Eq. (5)), this in turn reduces the growth of the return to one unit of efficiency, w^s .¹³

4.6.2. Step 2: The offspring of indigenous unskilled parents

In contrast to the offspring of the indigenous skilled who always invest in education, the offspring of the indigenous unskilled do not invest in human capital as long as the following inequality holds:

$$E^{us} w_{t+1}^s (1-\tau) - \theta w_t^s (1+r) < (2+r) w^m \left(\frac{E^{us} w_{t+1}^s (1-\tau)}{w^m} \right)^\beta. \quad (21)$$

Once this inequality is reversed (or turns into equality), children of indigenous unskilled parents choose to switch to skilled status.

¹² In the absence of redistribution ($\varphi=0$), fertility among the unskilled minority individuals is $N^m = (\beta/\delta)(2+r)$.

¹³ An assumption that $\beta > \delta(1 - (\theta w_t^s (1+r)/E^s w_{t+1}^s (1-\tau)))^{-1}$ ensures that the population of the skilled grows over time and thereby rules out the possibility of negative growth.

As one can immediately observe, their decision depends on the taxes levied on the skilled. Re-arranging Eq. (21), the necessary and sufficient condition for the offspring of the local unskilled to invest in human capital and switch to the skilled status is

$$(E^{us} w_{t+1}^s (1-\tau))^{1-\beta} - \frac{\theta w_t^s (1+r) E^{us}}{(E^{us} w_{t+1}^s (1-\tau))^\beta} \geq (2+r)(w^u)^{1-\beta}. \quad (22)$$

Notice that in any period $t+1$ the RHS of the above inequality is fixed and the LHS is decreasing in τ and increasing in w_{t+1}^s . If the return to one unit of efficiency (w^s) increases with time (Step 1), whereas the rate of tax (τ) is fixed, the LHS of Eq. (21) increases with time. It ensures that the increasing LHS of Eq. (22) will once exceed the fixed RHS of that equation. This intersection between the LHS and the RHS of Eq. (22) specifies the point where inequality (21) turns into equality. This point is crucial in the story. When inequality (21) is reversed, the offspring of the local unskilled find it lucrative to invest in education, acquire human capital, and switch to the skilled status. The redistribution policy, however, postpones the date of the switch.

The negative effect of the redistribution to the minority individuals on the local unskilled is twofold. First, taxation decreases their potential after-tax income in the skilled sector thereby directly reducing the profitability of investment in human capital. Second, through its negative effect on the aggregate human capital stock, it decreases the rate of growth in the return to efficiency labor thereby distorting the mechanism that eventually would make the acquisition of human capital worthwhile for the offspring of indigenous unskilled parents. This deters the investment in human capital that would transform indigenous low-income people to make them part of the skilled high-income population.¹⁴

This effect of the redistribution in favor of minorities thus provides a purely economic reason for inter-ethnic tensions observed in modern societies without reference to racial sentiments. Moreover, although the burden of taxation is not levied on the unskilled workers, the effect of redistribution on the offspring of the local unskilled is in a sense stronger than the effect on the offspring of the skilled, who by assumption always acquire education. This may contribute to a better understanding why the negative sentiments toward several minorities are particularly strong among the less prosperous segments of the indigenous population, as has been widely established empirically (Bauer, et al. 2000; Scheve and Slaughter, 2001; Dustmann and Preston, 2001, 2006, 2007; O'Rourke and Sinnott, 2006).

4.6.3. Step 3: The offspring of minority unskilled parents

Proceed now to the offspring of the minority unskilled. As long as the following inequality holds, they do not invest in human capital:

$$E^{ms} w_{t+1}^s - \theta w_t^s (1+r) < (w^m (2+r) + \varphi_{t+1}) \left(\frac{E^{ms} w_{t+1}^s}{w^m} \right)^\beta. \quad (23)$$

Once this inequality is reversed (or turns into equality), children of the minority unskilled parents choose to switch to skilled status.

As one can immediately observe, their decision directly depends on the transfer payments they receive. From Eq. (23), the critical value of the subsidy sufficiently high to prevent them from switching to skilled status is

$$\varphi_{t+1}^{crit} = (E^{ms} w_{t+1}^s - \theta w_t^s (1+r)) \left(\frac{E^{ms} w_{t+1}^s}{w^m} \right)^{-\beta} - w^m (2+r). \quad (24)$$

If the return in the skilled sector (w^s) grows over time (Step 1), Eq. (24) implies that the critical value of the transfer that prevents the minority unskilled from acquiring education increases with time.

Consider now the behavior of the transfers they actually receive. In Section 4.5 it has been shown that the number of the minority recipients increases faster than the number of the taxpaying local skilled. If the rate of increase in w^s is not too fast, transfer payments per capita must thus go down until the point when it becomes lucrative for the unskilled to acquire education, switch to the skilled status and increase the tax base.¹⁵ Thereafter, due to the higher fertility among the minority recipients, the per-capita transfers decrease again. Therefore, at some point the transfers they actually receive and the critical value of the subsidy (Eq. (24)) must intersect. At this point, when the offspring of the minority unskilled choose to acquire education, the redistribution is abolished and the economy returns to the undistorted growth path.

Proceed now to the dynamics of the minority fertility. Because the minority's over-fertility is a result of the redistribution, it follows the same dynamic path as the transfer payments do. Namely, at the point when the redistribution starts, the minority fertility becomes higher than its natural rate and remains higher until the end of the redistribution, although it declines along with the per-capita transfers. At the same time, fertility among the contribution local skilled is lower than its natural level. The fertility gaps disappear only once the redistribution is abolished.

¹⁴ Moreover, given the optimal fertility choice among the skilled (Eq. (13)), if the tax rate is higher than $\hat{\tau} = 1 - (\beta \theta w_t^s (1+r) / ((\beta - \delta) E^s w_{t+1}^s))$ taxation may turn the growth of the return to efficiency labor to negative, thereby forcing the offspring of the local unskilled to remain unskilled forever.

¹⁵ Notice that a single jump of the transfers up due to a momentary transition of all local unskilled to skilled status is a result of the assumption that all local unskilled individuals are alike. Imposing some moderate heterogeneity in the u-group would replace this peak with a high constant segment.

5. Conclusion

I have used a growth model with endogenous fertility to show how income redistribution increases the fertility of the immigrants and lowers fertility in the indigenous skilled population that finances the income transfers, with the result that human capital accumulation and the growth of per-capita output decline. Low-skilled immigration is the impetus for the decline in the incomes and numbers of the indigenous population. The conclusions are obtained under conditions in which immigrants do not compete in the local labor market with indigenous low-skilled workers. The indigenous low-skilled workers also do not pay taxes to finance income transfers to immigrants. Nonetheless indigenous low-skilled workers lose from the presence of immigrants.

I have shown how the source of the loss for indigenous low-skilled workers is traced to the relationship between fertility and human capital investment. There are two sources of the disadvantageous consequences for indigenous unskilled people. Taxation of income of the skilled population directly decreases their potential after-tax income in the skilled sector. Taxation also reduces the rate of increase in the return to efficiency labor, thereby distorting the mechanism that eventually would make the acquisition of human capital worthwhile for the offspring of indigenous unskilled parents, which deters the investment in human capital that would transform indigenous low-income people to make them part of the skilled high-income population.

More generally, I have presented a model that is based on empirical foundations and predicts if trends continue the decline of the west, in particular in Europe, because of the longer-run consequences of unskilled dependent immigration.

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